STRUCTURE OF THE COURSE : B. SC. III MATHEMATICS B. Sc. Part-III Mathematics (CBCS) Syllabus w. e. f. June 2020

SEMESTER - V B.Sc. III

Sr.	Subject Title	Paper	Theory		Pra ctical	
No.		Code/Number	No. of	Credits	No. of	Credits
			Lectures		Lectures	
1	Mathematical Analysis	BMT 501	3	2	•••	•••
2	Abstract Algebra	BMT 502	3	2	•••	•••
3	Optimization Techniques	BMT 503	3	2	•••	•••
4	Elective I	BMT 504	3	2	•••	
5	Practical Paper-V	BMP505	•••		10	4
6	Practical Paper-VI	BMP506	•••		10	4
7	Analytical	SECC-I	1	1	3	1
	Geometry					
8	AECC-1E	III	2	2	•••	
	Total		15	11	23	09

Semester - VI

Sr.	Subject Title	Paper	Theory		Practical	
No.		Code/Number	No. of Lectures	Credits	No. of Lectures	Credits
1	Metric Spaces	BMT 601	3	2	•••	•••
2	Linear Algebra	BMT 602	3	2	•••	•••
3	Complex Analysis	BMT 603	3	2	•••	
4	Elective I	BMT 604	3	2	•••	•••
5	Practical Paper VII	BMP605			10	4
6	Practical Paper VIII	BMP606	•••	•••	10	4
7	Entrepreneurship Development Program	SECC-II	1	1	3	1
8	AECC-1F	IV	2	2		
	Total		15	11	23	09

47

B.Sc.

- ◆ Total marks for B.Sc. Part –III including skill and AECC = 800·
- Total credit for B.Sc. part-III semester V and VI = 40
- ♦ AECC-Ability Enhancement Compulsory Course (1E & 1F)- English
- SECC Skill enhancement course for each subject

BMT501: Mathematical Analysis Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objectives : Students should

- 1. integrates the bounded function on a closed and bounded interval.
- 2. understand families and properties of Riemann integrable functions.
- 3. apply the fundamental theorems of integration.
- 4. expansion the functions in Fourier series and half range Fourier series.

UNIT-I

1. Riemann Integration

Definition of Riemann integration and simple examples: norm of subdivision, lower and upper sum, lower and upper integrals, oscillatory sums, Riemann Integral. Inequalities for lower and upper Darboux sums, Necessary and sufficient conditions for Riemann integrability, Existence of Riemann integral.

UNIT - II

2. Properties of Riemann Integral

Algebra and properties of Riemann integrable functions, Primitive of a function, first and second fundamental theorems of integral calculus.

UNIT - III

3. Improper Integrals

Definition of improper integral of first kind, second kind, third kind and its examples, Comparison

Test, μ – test for Convergence, Absolute and conditional convergence, Integral test for convergence

48

[09]

[09]

[09]

of series, Definition of improper integral of second kind and some tests for their convergence, Cauchy Principle Value.

UNIT IV

4. Fourier series

[09]

Definition of Fourier series and examples on the expansion of functions in Fourier series, Fourier series Corresponding to even and odd functions, half range Fourier series, half range sine and cosine series

Course outcomes:

Unit - I : After completion, Students are able to:

- 1. describe fundamental properties of the Riemann integration and existence theorems.
- 2. understand necessary and sufficient conditions for Riemann integrability.

Unit - II : After completion, Students are able to:

- 1. understand the first and second theorem of Integral calculus.
- 2. define properties of Riemann integrable functions.

Unit - III : After completion, Students are able to:

- 1. understand the concepts of Improper integral.
- 2. explain difference between absolute and conditional convergence.

Unit - IV : After completion, Students are able to:

- 1. develop the functions in Fourier series.
- 2. define Fourier series Corresponding to even and odd functions.

Reference Books

1. First Course in Mathematical Analysis:

D Somasundaram and B Choudhary Narosa Publishing House New Delhi, Eighth Reprint 2013 (Chapter 8, Chapter 10, Art 10.1)

49

2. Elementary Analysis The Theory of Calculus:

Kenneth. A. Ross Second Edition, Undergraduate Texts in Mathematics, Springer, 2013. (Chapter 6, Art. 32.1 to 32.11, 33.1 to 33.6 and 34.1 to 34.4)

3. Methods of Real Analysis:

R. R. Goldberg, Oxford & IBH Publishing Co. Pvt. Ltd., New Delhi.

4. Introduction to Real Analysis:

R.G. Bartle and D. R. Sherbert, Wiley India Pvt. Ltd., Fourth Edition 2016.

5. Elements of Real Analysis:

Shanti Narayan and Dr. M. D. Raisinghania, S. Chand & Company Ltd. New Delhi, Fifteenth Revised Edition 2014.

6. A Course of Mathematical Analysis:

Shanti Narayan and P. K. Mittal, S.Chand& Company Ltd. New Delhi, Reprint 2016.

7. Real Analysis:

HariKishan, PragatiPrakashan, Meerut, Fourth Edition 2012. Mathematical Physics, H. K. Das, Rama Varma, S Chand Publishing, 2018.



BMT 502: Abstract Algebra Theory: 45 Lectures of 48 minutes (36 Hours)

(Credits: 02)

Course Objectives : Students should

- 1. understand basic concepts of group and rings with examples.
- 2. identify whether the given set with the compositions form Ring, Integral domain or Field.
- 3. learn concepts of Group and Ring.

UNIT - I : GROUPS

Definition and examples of groups, group S3 and Dihedral group D4, Commutator subgroups and its properties, Conjugacy in group and class equation.

UNIT - II : RINGS

Definition and examples of Rings, commutative ring, Non-commutative ring, Ring with unity, Ring with Zero divisor, Ring without zero divisor, Integral Domain, Division Ring, Field, Boolean ring, Subring, Characteristic of a ring: Nilpotent and Idempotent elements. Ideals, Sum of two ideals, Examples, Simple Ring.

UNIT - III : HOMOMORPHISM AND IMBEDDING OF RING [09]

Quotient Rings, Homomorphism, Kernel of Homomorphism, Isomorphism theorems, imbedding Of Ring, Maximal Ideals, Prime ideal, Semi-Prime Ideal.

UNIT - IV : POLYNOMIAL RING AND UNIQUE FACTORIZATION DOMAIN [09]

Polynomial Rings, degree of Polynomial, addition and multiplication of Polynomials and their properties, UFD, Gauss' Lemma.

51

Course outcomes:

Unit - I : After completion, Students are able to :

- 1. perform basic computations in group theory.
- 2. understand the concept of subgroups and its examples.

[09]

[09]

Unit - II : After completion, Students are able to :

- 1. apply fundamental theorem, Isomorphism theorems of groups to prove these theorems for Ring.
- 2. understand the concept of Maximal Ideals, Prime Ideals and its examples.

Unit - III : After completion, Students are able to:

- 1. apply fundamental theorem, Isomorphism theorems of Ring.
- 2. understand the concept of Ideals and its examples.

Unit - IV : After completion, Students are able to:

- 1. understand the concepts of polynomial rings, unique factorization domain.
- 2. perform addition and multiplication of Polynomials.

Reference Books

1. A Course In Abstract Algebra

Vijay K. Khanna, S.K. Bhambri, Vikas publishing House Pvt.Ltd., New –Delhi-110014, Fifth Edition 2016. (Chap.3 Art. The Dihedral Group, commutator, Chap. 4 Art. Conjugate elements, Chap.7 Art. Subrings, characteristic of a ring, Ideals, Sum of Ideals, Chap. 8 Art. Quotient rings, Homomorphism, Embedding of Rings, More on Ideal, Maximal Ideal, Chap 9 Polynomial Rings, Unique Factorization Domain.)

2. A First Course in Abstract Algebra Jonh B. Fraleigh, Pearson Education, Seventh Edition (2014).

3. Topics in Algebra

Herstein I. N, Vikas publishing House, 1979.

4. Fundamentals of Abstract Algebra

Malik D. S. Moderson J. N. and Sen M. K., Mc Grew Hill, 1997.

5. Basic Algebra

N. Jacobson, Vol. I & II, Freeman and Company, New York 1980.



BMT 503: Optimization Techniques Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objectives : Students should

- develop basic knowledge of Operations Research models and techniques, which 1 can be applied to a variety of industrial and real life applications.
- 2. formulate and apply suitable methods to solve problems.
- 3. identify and select procedures for various sequencing, assignment, transportation problems.
- 4 identify and select suitable methods for various games.
- 5. to apply linear programming and find algebraic solution to games.

UNIT-I : Linear Programming problems:

Introduction, Formulation of Linear Programming Problems., Graphical methods for Linear Programming Problems. General formulation of Linear Programming problems, Slack and surplus variables, Canonical form, Standard form of Linear Programming problems.

UNIT - II: Transportation:

Transportation problem:

Introduction, Mathematical formulation, Matrix form of Transportation Problem. Feasible solution, Basic feasible solution and optimal solution, Balanced and unbalanced Transportation problems.

Methods of Initial basic feasible solutions:

North west Corner rule [Steppingstone method], Lowest cost entry method [Matrix minima method]

UNIT - III : Assignment Problems Assignment Models:

Introduction, Mathematical formulation of assignment problem, Hungarian method for assignment problem. Unbalanced assignment problem. Travelling Salesman problem.

UNIT - IV : Game Theory

Game theory :

Basic definitions, Minimax [Maximin] Criterion and optimal strategy, Saddle point.optimal strategy and value of game. Solution of games with saddle point. Fundamental theorem of gametheory [Minimax theorem], Two by two (2×2) games without saddle point. Algebraic

53

[09]

[08]

[09]

[10]

method of Two by two $(2 \ 2)$ games. Arithmetic method of Two by two $(2 \ 2)$ games. Graphical method for $2 \times n$ games and m 2 games, Principle of dominance.

Course Outcomes:

UNIT - I : After completion of the unit, Students are able to :

- 1. understand importance of optimization of industrial process management.
- 2. solve Linear Programming Problems by using Graphical Method.

UNIT - II : After completion of the unit, Students are able to:

- 1. apply basic concepts of mathematics to formulate an optimization problem.
- 2. solve Balanced and unbalanced Transportation problems.

UNIT - III : After completion of the unit, Students are able to :

- 1. analyze and appreciate variety of performance measures for various optimization problems.
- 2. solve Travelling Salesman problem.

UNIT - IV : After completion of the unit, Students are able to:

- 1. find Saddle point of given game theory.
- 2. define Fundamental theorem of game theory

Reference books

- 1. "Theory Methods and Applications": Sharma S. D. Kedarnath, Ramnath Meerut, Delhi Reprint 2015.
- 2. Optimization Techniques : Mohan, C. and Deep, Kusum, Optimization Techniques, New Age, 2009.
- **3. Optimization Methods in Operations, Research and Systems Analysis:** Mittal, K. V. and Mohan, C., New Age, 2003.
- 4. **Operations Research An Introduction:** Taha, H.A., Prentice Hall, (7th. Edition), 2002
- Operations Research: Principles and Practice: Ravindran, A. Phillips, D. T and Solberg, J. J., John Willey and Sons, 2nd Edition, 2009.
- 6. Operation Research: Theory and Applications: J. K. Sharma, Laxmi Publications, 2017.
- 7. Operation Research: Kanti Swarup, P. K. Gupta and Manmohan, S. Chand& Co.
- 8. Linear programming:G. Hadley Oxford and IBH Publishing Co.



BMT 504(A): Numerical Methods-I Theory: 45Lectures (48minutes)(36 Hours) (Credits: 02)

Course Objectives : Students should

- 1. use appropriate numerical methods and determine the solutions to given non-linear equations.
- 2. use appropriate numerical methods and determine approximate solutions to systems of linear equations.
- 3. use appropriate numerical methods and determine approximate solutions to ordinary differential equations.
- 4. demonstrate the use of interpolation methods to find intermediate values in given graphical and/or tabulated data.

UNIT-I:

NON-LINEAR EQUATIONS

Introduction: Polynomial equations, algebraic equations and their roots, iterative methods, Bisection method, algorithm, examples, Secant method: iterative sequence of secant method, examples, Regula-Falsi method: algorithm, graphical representation, examples. **Newton's method:** algorithm, examples.

UNIT-II:

SYSTEM OF LINEAR EQUATIONS: EXACT METHODS [09]

Introduction: System of linear equations as a vector equation Ax = b, Augmented matrix Direct methods: Gauss elimination method: Procedure, examples, Gauss-Jordan method: Procedure, examples. Iterative methods: General iterative rule.

UNIT - III :

SYSTEM OF LINEAR EQUATIONS: ITERATIVE METHOD [09]

Jacobi iteration scheme, examples, Gauss-Seidel method: Formula, examples.

UNIT-IV:

EIGENVALUES ANA EIGENVECTORS

Eigen values and eigenvectors of a real matrix, Power method for finding an eigenvalue of greatest modulus, the case of matrix whose "dominant eigenvalue is not repeated", examples, Method of exhaustion, examples, Method of reduction, examples. Shifting of the eigen value, examples.

55

[09]

[09]

Course Outcomes:

Unit - I : After completion, Students are able to

- 1. derive numerical methods for various mathematical operations and tasks, such as Secant method Gauss-Seidel method, Regula-Falsi method the solution of differential equations.
- 2. analyze and evaluate the accuracy of common numerical methods.

Unit - II : After completion, Students are able to

- 1. explain procedure of Gauss elimination and Gauss Jordan method.
- 2. solve system of linear equations by using Gauss elimination and Gauss Jordan method.

Unit - III : After completion, Students are able to

- 1. solve system of linear equations by using Jacobi Iteration method.
- 2. solve system of linear equations by using Gauss-Seidel method.

Unit - IV : After completion, Students are able to

- 1. use power method to find eigenvalue of greatest modulus.
- 2. find Eigen values and eigenvectors of a real matrix.

Reference Books

- 1. An Introduction to Numerical Analysis: Devi Prasad, Narosa Publishing House(Third Edition)
- 2. Introductory Methods of Numerical Analysis : S. S. Sastry, Prentice Hall of India.
- 3. Numerical Methods for Mathematics : J.H. Mathews, Science and Engineering, Prentice Hall of India.
- Numerical Methods for Scientists and Engineers :
 K. Sankara Rao, Prentice Hall of India.
 Numerical Analysis: Bhupendra Singh, Pragati Prakashan



BMT 504(B): Integral Transforms Theory: 45 Lectures (48 minutes) (36 Hours) (Credits: 02)

Course Objectives : Students should

- 1. understand the concept of Laplace Transform.
- 2. apply properties of Laplace Transform to solve differential equations.
- 3. understand relation between Laplace and Fourier Transform.
- 4. understand infinite and finite Fourier Transform.
- 5. apply Fourier transform to solve real life problems.

UNIT - I : Laplace Transform

Laplace Transform :

Definitions; Piecewise continuity, Function of exponential order, Function of class A, Existence theorem of Laplace transform. Laplace transform of standard functions. First shifting theorem and Second shifting theorem and examples, Change of scale property and examples, Laplace transform of derivatives and examples, Laplace transform of integrals and examples. Multiplication by power of t and examples. Division by t and examples. Laplace transform of Heaviside's unit Step function

Unit - II :

Inverse Laplace Transform : Inverse Laplace Transform:

Definition, Standard results of inverse Laplace transform, Examples, First shifting theorem and Second shifting theorem and examples. Change of scale property and Inverse Laplace of derivatives, examples. The Convolution theorem and Multiplication by S, examples. Division by S, inverse Laplace by partial fractions, examples, Solving linear differential equations with constant coefficients by Laplace transform.

Unit - III : Infinite Fourier Transform:

The infinite Fourier transform and inverse: Definition, examples, Infinite Fourier sine and cosine transform and examples. Definition: Infinite inverse Fourier sine and cosine trans form and examples. Relationship between Fourier transform and Laplace transform. Change of Scale Property and examples. Modulation theorem. The Derivative theorem. Extension theorem. Convolution theorem and examples.



[09]

[09]

[09]

Unit - IV :

B.Sc.

Finite Fourier Transform:

[09]

Finite Fourier Transform and Inverse, Fourier Integrals, Finite Fourier sine and cosine transform with examples. Finite inverse Fourier sine and cosine transform with examples. Fourier integral theorem. Fourier sine and cosine integral (without proof) and examples.

Course Outcomes:

Unit I: After completion of the unit, students are able to

- 1. recognize the different methods of finding Laplace transforms and Fourier transforms of different functions.
- 2. find Laplace transform of periodic functions and examples.

Unit - II : After completion of the unit, students are able to

- 1. calculate inverse Laplace by partial fractions.
- 2. use first shifting theorem and Second shifting theorem.

Unit - III : After completion of the unit, students are able to

- 1. use Infinite Fourier transform and inverse.
- 2. explain relationship between Fourier transform and Laplace transform.

Unit - IV : After completion of the unit, students are able to

- 1. apply methods of solving differential equations, partial differential equations, IVP and BVP using Laplace transforms and Fourier transforms.
- 2. apply the knowledge of L. T, F. T, and Finite Fourier transforms in finding the solutions of differential equations, initial value problems and boundary value problems.

Reference Books :

1. Laplace and Fourier Transform

J. K. Goyal, K. P. Gupta, A Pragati Edition (2016).

- 2. Integral Transform Dr. S. Shrenadh, S. Chand Prakashan.
- **3.** Integral Transforms and Their Applications B. Davies, Springer Science Business Media LLC (2002).
- 4. Laplace Transforms Murray R. Spiegel, Schaum's outlines.



[09]

[09]

BMT 504(C):Applications of Mathematics in Finance Theory: 45 Lectures (48 minutes) (36 Hours) (Credits: 02)

Course Objectives : Students should

- 1. understand the basic concepts in linear algebra, relating to linear equations, matrices, and optimization.
- 2. understand the concepts relating to functions and annuities.
- 3. apply Employ methods related to these concepts in a variety of financial applications.
- 4. apply logical thinking to problem solving in context.
- 5. use appropriate technology to aid problem solving.

UNIT - I : FINANCIAL MANAGEMENT

An overview, Nature and Scope of Financial Management. Goals of Financial Management and main decisions of financial management. Difference between risk, speculation and gambling.

UNIT - II: TIME VALUE OF MONEY

Interest rate and discount rate, Present value and future value, discrete case as well as continuous compounding case, Annuities and its kinds, Meaning of return, Return as Internal rate of Return (IRR), Numerical Methods like NewtonRaphson Method to calculate IRR, Measurement of returns under uncertainty situations, Meaning of risk, difference between risk and uncertainty, Types of risks. Measurements of risk, Calculation of security and Portfolio Risk and Return - Markowitz Model, Sharpe's Single Index Model, Systematic Risk and Unsystematic Risk.

UNIT - III : TAYLOR SERIES AND BOND VALUATION

Calculation of Duration and Convexity of bonds.

UNIT - IV : INANCIAL DERIVATIVES

Futures, Forward, Swaps and Options, Call and Put Option, Call and Put Parity Theorem. Pricing of contingent claims through Arbitrage and Arbitrage.

[09]

[09]

Course Outcomes:

Unit - I : After completion of the unit, students are able to

- 1. apply employ methods related to these concepts in a variety of financial applications.
- 2. understand scope of Financial Management.

Unit - II : After completion of the unit, students are able to

- 1. understand the concepts relating to functions and annuities.
- 2. understand types of risks.

Unit - III : After completion of the unit, students are able to

- 1. define convexity of bonds.
- 2. computation of calculation of Duration.

Unit - IV: After completion of the unit, students are able to

- 1. calculate Swaps and Options.
- 2. apply Parity Theorem.

References :

1. Corporate Finance - Theory and Practice:

Aswath Damodaran, John Wiley & Sons. Inc. John C. Hull, Options, Futures, and Other Derivatives, Prentice - Hall of India Private Limited.

2. An Introduction to Mathematical Finance:

Sheldon M. Ross, Cambridge University Press

3. Introduction to Risk Management and Insurance:

Mark S. Dorfman, Prentice Hall, Englwood Cliffs, New Jersey.



SECC: Analytical Geometry

Theory: 23 Lectures (48 minutes) (18 Hours)

Course Objective : Students should

- 1. introduce the geometry of lines and conics in the Euclidean plane.
- 2. develop geometry with a degree of confidence and will gain fluency in the basics of Euclidean geometry.
- 3. take foundational mathematical training.

Unit - I : Sketching Techniques

[12]

[11]

[12]

Techniques for sketching parabola, ellipse and hyperbola. Reflection properties of parabola, ellipse and hyperbola.

UNIT - II : Classification of Quadratic Equations

Classification of quadratic equations representing lines, parabola, ellipse and hyperbola.

UNIT - III : Surfaces

Spheres, Cylindrical surfaces. Illustrations of graphing standard quadric surfaces like cone, ellipsoid.

Course Outcomes:

Unit - I : After completion of the unit, students are able to

- 1. define parameterize the curves.
- 2. evaluate the distance and angle.

Unit - II : After completion of the unit, students are able to

- 1. sketch conic sections.
- 2. identify conic sections.

Unit - III : After completion of the unit, students are able to

- 1. determine congruent conics.
- 2. evaluate standard quadratic surfaces.

Reference Books:

- 1. Calculus : G.B. Thomas and R.L. Finney, 9th Ed., Pearson Education, Delhi, 2005.
- 2. Calculus : H. Anton, I. Bivens and S. Davis, John Wiley and Sons (Asia) Pvt. Ltd., 2002
- **3.** The Elements of Coordinate Geometry : S. L. Loney, McMillan and Company, London.
- **4.** Elementary Treatise on Coordinate Geometry of Three Dimensions: R.J.T. Bill, McMillan India Ltd., 1994.



BMP 505: Practical

Paper - V

Course Objectives: Student should

- 1. develop basic knowledge of Operations Research models and techniques, which can be applied to a variety of industrial and real life applications.
- 2. formulate and apply suitable methods to solve problems.
- 3. identify and select procedures for various sequencing, assignment, transportation problems.
- 4. identify and select suitable methods for various games.
- 5. to apply linear programming and find algebraic solution to games.

Experiments

- 1. Simplex Method : Maximization Case
- 2. Simplex Method : Minimization Case
- 3. Two-Phase Method
- 4. Big-M-Method
- 5. North- West Corner Method
- 6. Least Cost Method
- 7. Vogel's Approximation Method
- 8. Optimization of T.P. by Modi Method
- 9. Hungarian Method
- 10. Maximization Case in Assignment Problem
- 11. Unbalanced Assignment Problems
- 12. Travelling Salesman Problem
- 13. Games with saddle point
- 14. Games without saddle point : (Algebraic method)
- 15. Games without saddle point : a) Arithmetic Method b) Matrix Method
- 16. Games without saddle point : Graphical method

Course Outcomes : After completion, students are able to

- 1. understand importance of optimization of industrial process management.
- 2. apply basic concepts of mathematics to formulate an optimization problem.
- 3. analyze and appreciate variety of performance measures for various optimization problems.

Reference Books :

- 1. Operations Research [Theory and Applications], By J.K.Sharma Second edition, 2003, Macmillan India Ltd., New Delhi.
- 2. Operations Research: S. D. Sharma.

62

BMP 506: Practical Paper - VI

Course Objectives : Student should

- 1. use appropriate numerical methods and determine the solutions to given non-linear equations.
- 2. use appropriate numerical methods and determine approximate solutions to systems of linear equations.
- 3. use appropriate numerical methods and determine approximate solutions to ordinary differential equations.
- 4. demonstrate the use of interpolation methods to find intermediate values in given graphical and/or tabulated data.

Experiments

- 1. Bisection method
- 2. Secant method
- 3. Newton's method
- 4. Gauss elimination method Two-Phase Method
- 5. Gauss-Jordan method.
- 6. Jacobi iteration scheme
- 7. Gauss-Seidel method
- 8. Power method
- 9. Newton's forward interpolation
- 10. Newton's backward interpolation
- 11. Lagrangian interpolation
- 12. Divided difference interpolation
- 13. Trapezoidal rule
- 14. Simpson's 1/3rd rule
- 15. Second order Runge-Kutta method
- 16. Fourth order Runge-Kutta method

Course Outcomes: After completion, students are able to

- apply numerical methods to find the solution of algebraic equations using different 1. methods under different conditions.
- 2. numerical solution of system of algebraic equations.
- 3. apply various interpolation methods and finite difference concepts.
- 4. work out numerical differentiation and integration whenever and wherever routine methods are not applicable.

Reference books

1. An Introduction to Numerical Analysis : Devi Prasad, Narosa Publishing House (Third Edition)

2. **Introductory Methods of Numerical Analysis:**

S. S. Sastry, Prentice Hall of India.

3. **Numerical Methods for Mathematics:**

J. H. Mathews, Science and Engineering, Prentice Hall of India.

4. Numerical Methods for Scientists and Engineers:

K. Sankara Rao, Prentice Hall of India.

5. **Numerical Analysis:**

Bhupendra Singh, Pragati Prakashan.



B.Sc.III –Semester VI **BMT-601: Metric Spaces** Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objective : Students should

- 1. acquire the knowledge of notion of metric space, open sets and closed sets.
- 2. demonstrate the properties of continuous functions on metric spaces.
- 3. apply the notion of metric space to continuous functions on metric spaces.
- 4. understand the basic concepts of connectedness, completeness and compactness of metric spaces.
- 5. appreciate a process of abstraction of limits and continuity in metric spaces.

UNIT - I : LIMITS AND METRIC SPACES

Revision: Limits of a function on the real line, Metric space, Limits in Metric space.

UNIT -II : CONTINUOUS FUNCTIONS ON METRIC SPACES [9]

Continuity at a point on the real line, Reformulation, Functions continuous on a metric space, Open Sets, Closed Sets, Homeomorphism, dense subset of a metric space.

UNIT - III : CONNECTEDNESS, COMPLETENESS, AND COMPACTNESS

More about open sets, connected sets, Bounded and totally bounded sets, dense set, Complete metric space, contraction operator, Compact metric spaces, Covering and open covering, Borel property, Finite intersection property

UNIT - IV : SOME PROPERTIES OF CONTINUOUS FUNCTIONS ON METRICSPACES [9]

Continuous functions on compact metric spaces, Bounded function, Uniform continuity,

Course Outcomes :

UNIT - I : After completion, students are able to

- understand the Euclidean distance function on Rⁿ and appreciate its properties. 1.
- 2 understand the concept and examples of metric space.

UNIT - II: After completion, students are able to

- explain the definition of continuity for functions. 1.
- 2. understand the concept of open and closed sets.

65

[9]

[9]

UNIT - III : After completion, students are able to

- 1. explain the geometric meaning of each of the metric space properties (M1) (M3) and be able to verify whether a given distance function is a metric.
- 2. identify the dense set, Complete metric space, Compact metric spaces.

UNIT - IV: After completion, students are able to

- 1. distinguish between open and closed balls in a metric space and be able to determine them for given metric spaces.
- 2. check the continuity and uniform continuity on compact metric space.

References :

- 1. **Methods of Real Analysis** R.R.Goldberg, Oxford and IBH Publishing House, 2017.
- 2. **Mathematical Analysis** T. M. Apostol, Narosa Publishing House, 2002.
- 3. **Mathematical Analysis** Satish Shirali, H.L. Vasudeva, Narosa Publishing House, 2013
- First Course in Mathematical Analysis
 D. Somasundaram, B. Choudhary, Narosa Publishing House, 2018.
- 5. **Principles of Mathematical Analysis** W. Rudin, McGraw Hill Book Company, 1976.
- 6. **A Course of Mathematical Analysis** Shantinarayan, Mittal, S.Chand and Company, 2013.
- 7. **Mathematical Analysis I** J.N. Sharma, Krishna Prakashan Mandir, Meerut, 2014.

8. **Mathematical Analysis** S.C. Malik, SavitaArrora, New age international ltd, 2005.



BMT-602: Linear Algebra Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objectives : Students should

- 1. understand the notion of vector space...
- 2. work out algebra of linear transformations.
- 3. appreciate connection between linear transformation and matrices.
- 4. work out Eigen values, Eigen vectors and its connection with real life situation.

UNIT - I : Vector Spaces

Vector space, Subspace, Sum of subspaces, direct sum, Quotient space, Homomorphism or Linear transformation, Kernel and Range of homomorphism, Fundamental Theorem of homomorphism, Isomorphism theorems, Linear Span, Finite dimensional vector space, Linear dependence and independence, basis, dimension of vector space and subspaces.

UNIT - II : Linear Transformations

Linear Transformation, Rank and nullity of a linear transformation, Sylvester's Law, Algebra of Linear Transformations, Sum and scalar multiple of Linear Transformations. The vector space of homomorphism, Product (composition) of Linear Transformations, Linear operator, Linear functional, Invertible and non-singular Linear Transformation, Definition of Dual Space.

UNIT - III : Inner Product Spaces Inner product spaces:

Norm of a vector, Cauchy- Schwarz inequality, Orthogonality, Pythagoras Theorem, orthonormal set, Gram-Schmidt orthogonalization process, Bessel's inequality

UNIT - IV : Eigen values and Eigen vectors

Eigen values and Eigen vectors: Eigen space, Characteristic Polynomial of a matrix and remarks on it, similar matrices, Characteristic Polynomial of a Linear operator, Examples on eigenvalues and eigenvectors.



[9]

[9]

[9]

[9]

Course Outcomes:

UNIT - I : After completion, students are able to

- 1. explain the concepts of basis and dimension of a vector space.
- 2. explain the concept of kernel and range of homomorphism.

UNIT - II : After completion, students are able to

- 1. explain the properties of vectors.
- 2. check invertible and non-singular Linear Transformation.

UNIT - III: After completion, students are able to

- 1. explain the Inner product spaces and check whether the set is orthonormal.
- 2. explain Gram-Schmidt orthogonalization process.

UNIT - IV: After completion, students are able to

- 1. understands eigenvalues, eigenfunctions, Characteristic Polynomial of a matrix.
- 2. find the eigenvalues and eigenvectors.

References :

- 1. A Course in Abstract Algebra, Khanna V. K. and Bhambri S. K., Vikas Publishing House PVT Ltd., New Delhi, 5th edition,2016.
- Elementary Linear Algebra (with Supplemental Applications), H. Anton & C.Rorres, Wiley India Pvt. Ltd (Wiley Student Edition), New Delhi, 11th Edition 2016.
- Linear Algebra,
 S. Friedberg, A. Insel, L. Spence, Prentice Hall of India, 4th Edition, 2014.
- 4. Linear Algebra, Holfman K. and Kunze R,Prentice Hall of India, 1978.
- 5. Linear Algebra, Schaum's Outline Series, Lipschutz S, McGraw Hill, Singapore, 1981.

Linear Algebra and its Applications, David Lay, Steven Lay, Judi McDonald, Pearson Education Asia, Indian Reprint, 5th Edition, 2016.



Mathematics

BMT-603: Complex Analysis Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objective: Students should

- 1. learn basic concepts of functions of complex variable.
- 2. introduce the concept of analytic functions.
- 3. learn concept of complex integration.
- 4. introduce the concepts of sequence and series of complex variable.
- 5. learn and apply concept of residues to evaluate certain real integrals.

UNIT - I : Analytic functions

Limit and continuity of a function of a complex variable, complex valued function. Differentiability and continuity and elementary rules of Differentiation. Analytic function and Analytic function in domain. Necessary and sufficient condition for F(z) = u+iv to be Analytic and examples, Limit of a sequence of complex numbers, Polar form of Cauchy-Riemann Equation, harmonic function, conjugate harmonic function, construction of Analytic function of analytic function.

UNIT - II : Complex Integration

Elementary Definitions, complex line integral, Integral along oriented curve and examples, Cauchy's integral theorem and its consequences, Cauchy's integral formula for multiply connected domain and its examples, Jordan curve, orientation of Jordan curve, simple connected and multiply connected domain, rectifiable curve and their properties. Higher order derivative of an analytic function,

UNIT - III : SINGULARITIES AND RESIDUES

Development of an analytic function as a power series, Taylor's theorem for complex function, Examples on Taylor's and Laurent series, Zeros of an analytic function, singular point, different types of singularity, poles and zeros, limiting point of zeros and poles. Residue theorem, residue at a pole and residue at infinity. Cauchy's residue theorem, computation of residue at a finite pole. Integration round unit circle, Jordan's lemma, Evaluation of Integrals

 $\int_{-\infty}^{\infty} f(z) dz$ when f(z) has no poles on the real line and when poles on the real line.

[9]

[9]

[9]

UNIT - IV : ENTIRE MEROMORPHIC FUNCTIONS

[9]

Definition of entire and meromorphic functions. Characterization of polynomials as entire functions, Characterization of rational functions as meromorphic functions, Mittag-Leffler's expansion, Rouche's theorem and solved problems. Some theorems on poles and singularities.

References :

- 1. **Complex Variables and Applications**, James Ward Brown and Ruel V.Churchill, McGraw – Hill Education (India) Edition,
- 8th Ed.2014, Eleventh reprint 2018.
 Foundations of Complex Analysis, S.Ponnusamy, Narosa Publishing House, Second Edition, 2005, Ninth reprint 2013.
- 3. **Complex Analysis**, Lars V Ahlfors, McGraw-Hill Education, 3 edition, January 1, 1979.

Course Outcomes:

UNIT - I : After completion, students are able to

- 1. define the concept of derivation of analytic functions.
- 2. solved problems related to the test of analyticity of functions.

UNIT -II : After completion, students are able to

- 1. calculate the analytic functions.
- 2. understands the concept of Jordan curve, orientation of Jordan curve, rectifiable curve and it's properties.

UNIT - III : After completion, students are able to

- 1. express the power series expansion of analytic functions.
- 2. evaluate the integrals $\int_{-\infty}^{\infty} f(z) dz$ when f(z) has no poles on the real line and when poles on the real line.

UNIT - IV : After completion, students are able to

- 1. define the concept of Cauchy Goursat Integral Theorem.
- 2. understands the Rouche's theorem and problems on it.

70

BMT-604(A): Numerical Methods-II Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objective : Students should

- 1. analyze the errors obtained in the numerical solution of problems.
- 2. understand the common numerical methods and how they are used to obtain approximate solutions.
- 3. derive numerical methods for various mathematical operations and tasks, such as interpolation, differentiation, integration, the solution of linear and nonlinear equations, and the solution of differential equations.

UNIT - I : INTERPOLATION: EQUAL INTERVALS [9]

Forward interpolation:

Newton's forward differences, forward difference tableNewton's forward form of interpolating polynomial (formula only), examplesBackward interpolation: Newton's backward differences, backward difference table, Newton's backward form of interpolating polynomial (formula only), examples

UNIT-II: INTERPOLATION: UNEQUAL INTERVALS [9]

Introduction, Lagrangian interpolating polynomial (formula only), examples, Divided difference interpolation, Newton's divided differences, divided difference table, examples (finding divided differences of given data), Newton's divided difference form of interpolating polynomial, examples

UNIT - III : NUMERICAL DIFFERENTIATION AND INTEGRATION [9]

Numerical differentiation based on interpolation polynomial. Numerical integration:

Newton-Cotes formula (statement only), Basic Trapezoidal rule (excluding the computation of error term), composite Trapezoidal rule, examples, Basic Simpson's 1/3rd rule (excluding the computation of error term), composite Simpson's 1/3rd rule, examples. Basic Simpson's 3/8th rule (excluding the computation of error term), composite Simpson's 3/8th rule, examples.

UNIT - IV : ORDINARY DIFFERENTIAL EQUATIONS [9]

Euler's Method, Examples, Second order Runge-Kutta method (formula only), examples Fourth order Runge-Kutta method (formula only), examples

Course Outcomes:

UNIT - I : After completion, students are able to

- 1. apply numerical methods to find the solution of algebraic equations using different methods under different conditions.
- 2. find the numerical solution of system of algebraic equations.

UNIT - II : After completion, students are able to

- 1. apply various interpolation methods.
- 2. find numerical solutions.

UNIT - III : After completion, students are able to

- 1. work out numerical differentiation and integration whenever and wherever routine methods are not applicable.
- 2. apply basic Trapezoidal rule, basic Simpson's 1/3rd rule, basic Simpson's 3/8th rule.

UNIT - IV: After completion, students are able to

- 1. apply Euler's Method and find numerical solutions.
- 2. apply Second order Runge-Kutta method, Fourth order Runge-Kutta method and find numerical solutions.

References :

- 1. **An Introduction to Numerical Analysis**, Devi Prasad, Narosa Publishing House, Third Edition.
- 2. Introductory Methods of Numerical Analysis, S. S. Sastry, Prentice Hall of India.
- 3. Numerical Methods for Mathematics, Science and Engineering, J.H. Mathews, Prentice Hall of India.
- 4. Numerical Methods for Scientists and Engineers, K. SankaraRao, Prentice Hall of India.
- 5. **Numerical Analysis**, Bhupendra Singh, Pragati Prakashan.





BMT-604(B): Discrete Mathematics Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objective : Students should

- use classical notions of logic: implications, equivalence, negation, proof by contradiction, 1. proof by induction, and quantifiers.
- 2. apply notions in logic in other branches of Mathematics.
- Know elementary algorithms : searching algorithms, sorting, greedy algorithms, and 3. their complexity.
- 4. apply concepts of graph and trees to tackle real situations.
- 5. appreciate applications of shortest path algorithms in computer science.

UNIT - I : Mathematical Logic

The logic of compound statements: Statements, compound statements, truth values, logical equivalence, tautologies and contradictions. Conditional statements: Logical equivalences involving implication, negation. The contra positive of a conditional statement, converse, inverse of conditional statements, biconditional statements.

UNIT - II : Valid and Invalid Arguments

Modus Ponens and modus Tollens, Additional valid argument forms, rules of inferences, contradictions and valid arguments, Number system: Addition and subtraction of Binary, decimal, quintal, octal, hexadecimal number systems and their conversions.

UNIT - III : Graphs

Graphs:

Definitions, basic properties, examples, special graphs, directed and undirected graphs. concept of degree, Trails, Paths and Circuits: connectedness, Euler circuits, Hamiltonian circuits, Matrix representation of graphs, Isomorphism of graphs, isomorphic invariants, graph isomorphism for simple graphs.

UNIT - IV : Trees

Definitions and examples of trees, rooted trees, binary trees and their properties. spanning trees, Minimal spanning trees, Kruskal's algorithm, Prim's algorithm, Dijkstra's shortest path algorithm.

Course Outcomes: UNIT - I: After completion, students are able to

[9]

[9]

[9]

[9]

- 1. understand the notion of mathematical thinking, mathematical proofs and algorithmic
- thinking.apply mathematical thinking, mathematical proofs and algorithmic thinking. in problem

UNIT - II: After completion, students are able to

- 1. understand the basics of discrete probability.
- 2. understand Addition and subtraction of Binary, decimal, quintal, octal, hexadecimal number systems and their conversions.

UNIT - III : After completion, students are able to

- 1. understand the definition of graph and it's basic properties.
- 2. understand Matrix representation of graphs, Isomorphism of graphs, isomorphic invariants, graph isomorphism for simple graphs.

UNIT - IV : After completion, students are able to

- 1. understand the concept of trees, spanning trees.
- 2. apply Kruskal's algorithm, Prim's algorithm, Dijkstra's shortest path algorithm.

References :

- Discrete Mathematics with Applications, Susanna S. Epp, PWS Publishing Company, 1995. (Brooks/Cole, Cengage learning, 2011)
- 2. **Discrete Mathematics and its Applications**,Kenneth H. Rosen, McGraw Hill, 2002.
- 3. **Discrete Mathematical Structure with Applications**, J.P.Tremblay and R.Manohar, McGraw–Hill.
- 4. **Combinatorics: Theory and Applications**, V. Krishnamurthy, East-West Press.
- 5. **Discrete Mathematical Structures**, Kolman, Busby Ross, Prentice Hall International.
- 6. **Discrete Mathematical Structures**, R M Somasundaram, (PHI) EEE Edition 7.
- 7. **A Graduate Text in Computer Mathematics**, A.B.P.Rao and R.V.Inamdar, SUMS 1991.
- 8. **Discrete Mathematics**, Seymour Lipschutz and Marc Lipson, Schaum's Outlines Series, Tata McGraw -Hill.

74

B.Sc.

solving.

BMT-604(C): Applications of Mathematics in Insurance Theory: 45 Lectures of 48 minutes (36 Hours) (Credits: 02)

Course Objective : Students should

- 1. use statistics and probability theory together with mathematical analysis.
- 2. understand and do modeling in the various applications.
- 3. examine different risks that challenge our everyday lives.

UNIT-I: INSURANCEFUNDAMENTALS

Insurance, Meaning of loss, Chances of loss, peril, hazard and proximate cause in insurance. Costs and benefits of insurance to the society and branches of insurance .Life insurance and various types of general insurance.

UNIT - II : LIFE INSURANCE AND MATHEMATICS [9]

Insurable loss, exposures features of a loss that is ideal for insurance, Construction of Mortality Tables, Computation of Premium of Life Insurance for a fixed duration and for the whole life.

UNIT - III : DETERMINATION OF CLAIMS FOR GENERAL INSURANCE

Determination of claims for general insurance using Poisson distribution. Determination of claims for general insurance using Negative Binomial Distribution. The Polya Case

UNIT - IV : DETERMINATION OF THE AMOUNT OF CLAIMS IN **GENERAL INSURANCE** [9]

Compound Aggregate claim model and its properties, claims of reinsurance, Calculation of a compound claim density function, F-recursive and approximate formulae.

Course Outcomes

UNIT - I : After completion, students are able to

- understand the meaning of insurance. 1.
- 2. understand Costs and benefits of insurance to the society and branches of insurance.

75

[9]

[9]

UNIT - II : After completion, students are able to

- 1. illustrate the life insurance products.
- 2. construct Mortality Tables and compute Premium of Life Insurance for a fixed duration and for the whole life.

UNIT - III: After completion, students are able to

- 1. determine the claims for general insurance using Poisson distribution.
- 2. determine the claims for general insurance using Negative Binomial Distribution.

UNIT - IV: After completion, students are able to

- 1. understands the claims of reinsurance, F-recursive and approximate formulae.
- 2. calculate compound claim density function.

References :

- 1. **Corporate Finance Theory and Practice**, Aswath Damodaran, John Wiley & Sons.Inc.
- 2. **Options, Futures, and Other Derivatives**, John C. Hull, Prentice - Hall of India Private Limited
- 3. An Introduction to Mathematical Finance, Sheldon M.Ross, Cambridge University Press.
- 4. Introduction to Risk Management and Insurance, Mark S. Dorfman, Prentice Hall, Englewood Cliffs, New Jersey

76

SECC: Entrepreneurship Development Program (EDP) Theory: 24 lectures, 48 minutes (18 Hours)

Course Objective: Students should

- acquire necessary knowledge and skills required for organizing and carrying out 1. entrepreneurial activities
- 2. develop the ability of analyzing and understanding business situations in which entrepreneurs act and to master the knowledge necessary to plan entrepreneurial activities.
- 3. develop the ability of analyzing various aspects of entrepreneurship – especially of taking over the risk.

UNIT - I : Entrepreneurship, Creativity & Opportunities [10]

Concept, Classification & Characteristics of Entrepreneur, Creativity and Risk taking, Risk Situation, Types of risk& risk takers, Business Reforms, Process of Liberalization, Reform Policies, Impact of Liberalization, Emerging high growth areas, Business Idea Methods and techniques to generate business idea, Transforming Ideas in to opportunities transformation involves, Assessment of idea & Feasibility of opportunity SWOT Analysis

Information and Support Systems

Information needed and Their Sources :

Information related to project, Information related to support system, Information related to procedures and formalities, Support Systems Small Scale Business Planning, Requirements, Govt. & Institutional Agencies, Formalities Statutory Requirements and Agencies.

Market Assessment

Marketing-Concept and Importance Market Identification, Survey Key components Market Assessment.

UNIT - II : Business Finance & Accounts [10]

Business Finance-

Cost of Project Sources of Finance Assessment of working capital Product costing Profitability Break Even Analysis Financial Ratios and Significance

Business Account-

Accounting Principles, Methodology Book Keeping Financial Statements Concept ofAudit



Business Plan

Business plan steps involved from concept to commissioning, Activity Recourses, Time, Cost

Project Report :

Meaning and Importance, Components of project report/profile (Give list), Project Appraisal: 1) Meaning and definition 2) Technical, Economic feasibility 3) Cost benefit Analysis.

UNIT - III : Enterprise Management and Modern Trends [5] Enterprise Management: -

Essential roles of Entrepreneur in managing enterprise Product Cycle: Concept and importance Probable Causes of Sickness Quality Assurance: Importance of Quality, Importance of testing E-Commerce: Concept and Process.

Mathematics Entrepreneur:-

Assess yourself-are you an entrepreneur? Prepare project report for mathematics and study its feasibility.

Course Outcomes:

UNIT - I : After completion, students are able to

- 1. understand the concept of Entrepreneur.
- 2. know the Assessment of idea & Feasibility of opportunity SWOT Analysis.

UNIT - II : After completion, students are able to

- 1. analyze Financial Ratios and Significance.
- 2. understands the Methodology Book Keeping Financial Statements Concept of Audit.

UNIT - III : After completion, students are able to

- 1. manage the essential roles of Entrepreneur in product cycle.
- 2. understand Probable Causes of Sickness Quality Assurance.

References :

1. Entrepreneurship,

Alpana Trehan, Wiley India

2. A complete guide to successful Entrepreneurship,

G. N. Pandey., Vika



BMP-605: Mathematical Computation Using Python

Course Objective: Students should

- 1. learn the fundamentals of writing Python scripts.
- 2. write Python functions to facilitate code reuse.
- 3. use Python to read and write files.4. work with Python standard library.

Experiment

1. **Introduction to Python:**

Python, Anaconda, Spyder IDE, Python Identifiers and Keywords, data types, simple mathematical operation, Indentation and Comments., Input and Output, First Python program.

2. Expression and operators:

Expression, Boolean expression, logical operations: comparison operator, membership operator, identity operator, bitwise operator. Order of evaluation. File Handling: open, read, write, append modes of file.

3. Conditional Statements:

if-else, nested if-else, if-elif-else, try-except block.

4. Looping Statements, Control statements:

Looping Statements: for loop, while loop, Nested loops Control Statements: break, continue and pass.

5. Functions:

Built-in functions, User-defined functions, Arguments, recursive function, Python Anony mous/Lambda Function, Global, Local and Nonlocal variables and return statement.

6. Modules and packages in Python :

Modules, import, import with renaming, from-import statement, math module, cmath module, random module, packages.

 Python Data structure: Strings, list, tulpes, dictionary, set and array.

8. **Operations on set and array:**

Set operations, Intersection, union, difference, symmetric difference, searching and sorting.

79

9.	Systems of linear algebraic equations:		
	Gauss Elimination Method, LU Decomposition Methods		
10.	Roots of Equations:		
	Bisection, Newton-Raphson Method		

- 11. **Initial Value Problems :** Euler's Method, Runge-Kutta Methods.
- 12. Magic square and Area calculation without measurement.
- Graph Theory : Networkx
 Graph, nodes, edges, directed graph, multigraph, drawing graph, Google page rank
 by random walk method
- 14. Collatz conjecture and Monte Hall problem
- 15. Data compression using Number
- 16. Data visualization in Python:

2D and 3D plot in python: line plot, bar plot, histogram plot, scatter plot, pie plot, area plot, Mandelbrot fractal set visualization.

Course Outcomes:

After completion, students are able to

- 1. learn data types, simple mathematical operation, Indentation and Comments.
- 2. use if-else, nested if-else statement to write programs.
- 3. to solve system of linear algebraic equations.
- 4. to plot 2D and 3D plots, histogram plot, pie plot, area plot.

References :

- 1. **Python Programming**, John zele, third edition
- 2. **Python rocket reference**, Mark Lutz., Fifth edition.



BMP-606: Project, Study- Tour, Viva – Voce

A: Project

Each student of B.Sc. III is expected to read, collect, understand the culture of Mathematics, its historic development. He is expected to get adequate Mathematical concepts, innovations and relevance of Mathematics. Report of the project work should be submitted to the Department of Mathematics. Evaluation of the project report will be done by the external examiners at the time of annual examination.

B: Study Tour

It is expected that the tour should be arranged to visit the well-known academic institutions so that the students will be inspired to go for higher studies in Mathematics

C: SEMINARS

D: VIVA-VOCE (on the project report)